

## Chapter 35 - Externalities

→ An externality occurs when an economic agent is affected by the production or consumption decisions of other agent(s).

→ externalities may be positive or negative

e.g. Painting my house a pleasant color may confer positive externalities on my neighbors.

Painting my house a garish color may confer negative externalities on my neighbors.

→ consumption externalities stem from one agent's consumption decisions affecting another's production or consumption ~~decisions~~

→ e.g. you liking quiet at night may prevent your ~~roommate~~ roommate from producing ~~rock~~ music.

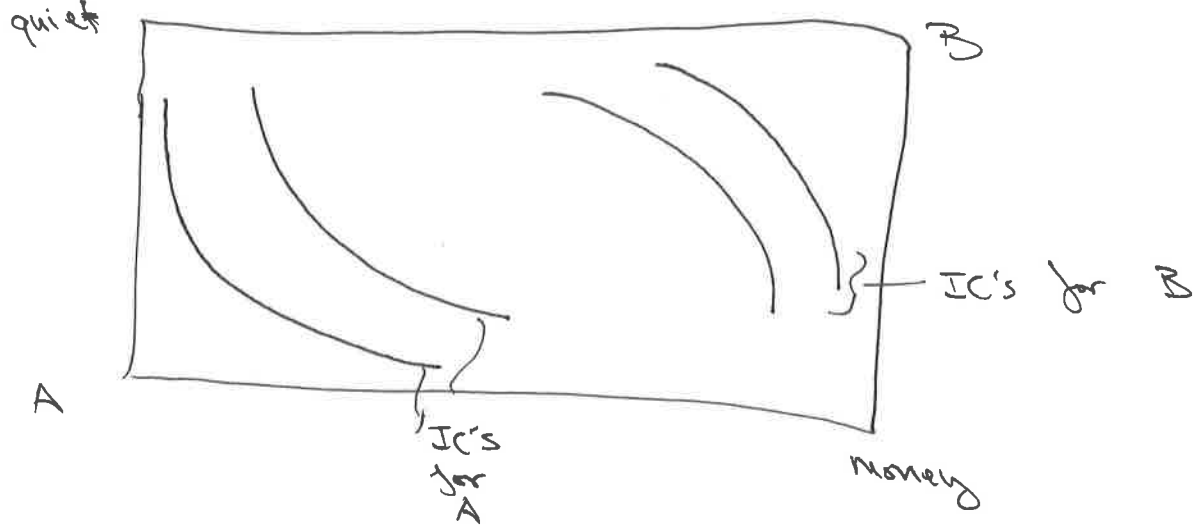
→ production externalities stem from one agent's production decisions affecting the production or consumption of others

→ e.g. band practice by your roommate may prevent you from consuming sleep

→ important point → it takes 2 (or more) to create an externality  
→ you wanting quiet and your roommate wanting to practice are both necessary  
→ it's no one's fault

# A market for externalities

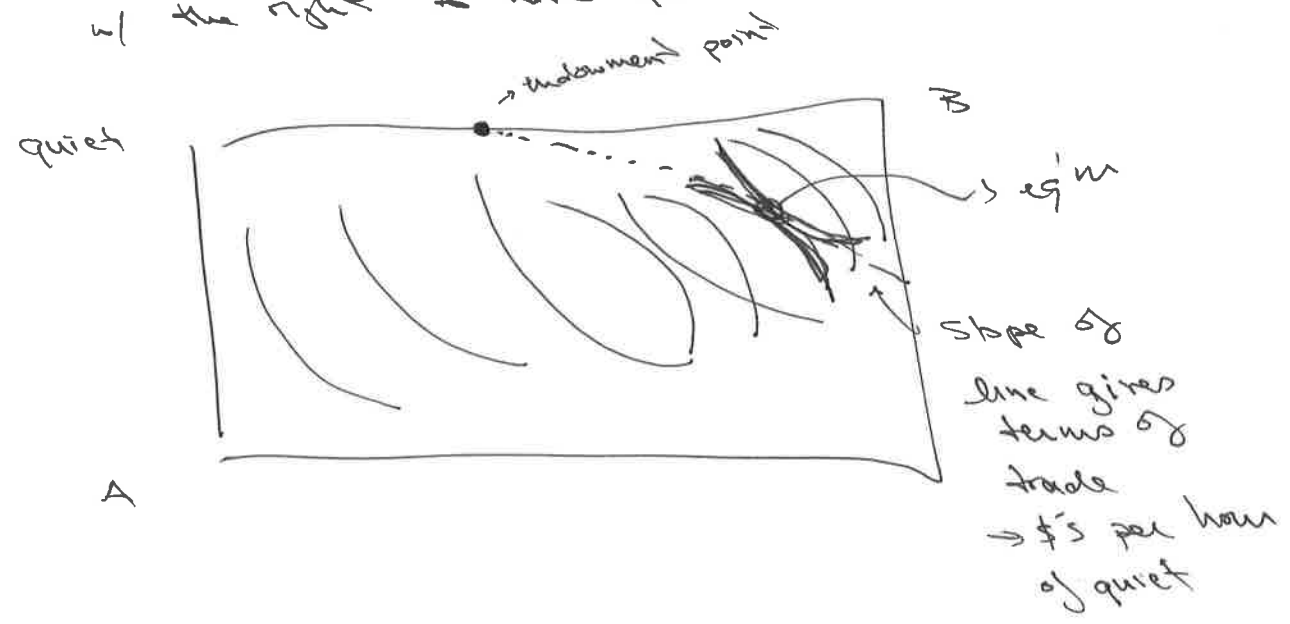
- extend this 2 roommate example - one who likes to sleep and the other who likes to practice w/ his band
- assume both have (and value) money. ~~and the~~
- roommate A values quiet hours
- roommate B values noisy hours (non-quiet for band practice)



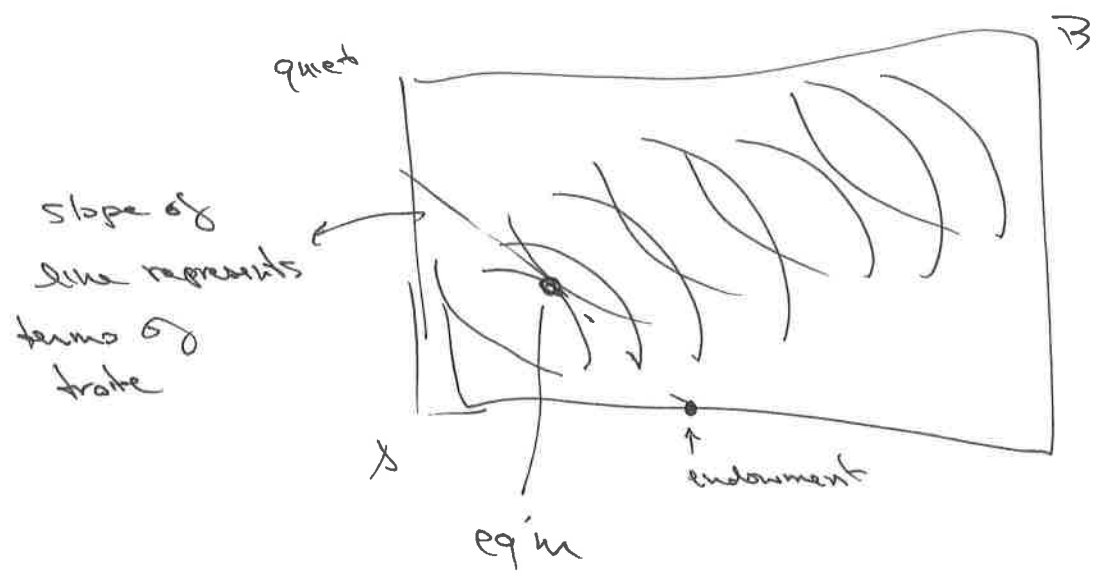
Edgeworth Box Diagram

- equilibria come where indiff curves are tangent:
  - this is where gains from trade are exhausted
- where these equilibria are located depends on what each roommate is endowed with

→ consider where both are endowed w/ \$100 and roommate A is endowed w/ the right to have quiet!



→ Now consider where both have \$100 and B is endowed w/ right to play music at any hour:



→ either way we have an eq'm  
 → either way the eq'm is pareto ~~optimal~~ optimal  
 → But distribution of outcome very different - depends on endowment

→ But main point - if can trade \$ for quiet - no efficiency lost from externality

⇒ Key: externalities are only a problem if there is no market for the externality

### The Coase Theorem

→ If can trade in externality and transactions costs are low, then bargaining leads to a Pareto efficient outcome regardless of the initial allocation of property rights.

→ This is what we saw w/ the roommate example

→ highlights importance of defining property rights

→ Coase's work has been extremely influential in law and economics field

# Production externalities

E.g.  
→ 2 producers, one who creates an externality

steel manufacturer/polluter

$$\max_{S, X} P_S S - C_S(S, X)$$

fishery ~~polluter~~

$$\max_P P_F F - C_F(Y, X)$$

↑  
affected by pollution,  
but can't determine/choose  
pollution

FOC's for steel producer:

$$P_S = \frac{\partial C_S(S, X)}{\partial S}$$

$$0 = \frac{\partial C_S(S, X)}{\partial X}$$

→ price for pollution is zero so produce a lot of it

FOC for fishery:

$$P_F = \frac{\partial C_F(Y, X)}{\partial Y}$$

→ production of steel/fish impose private costs on each firm

→ production of steel has an additional social cost - the cost to the fishery of producing steel

→ If the steel producer and fishery became one company, they would internalize the social cost. The joint company's profit max would be:

$$\text{Max}_{S, f, x} P_S S + P_f f - c_S(S, x) - c_f(f, x)$$

FOCs:

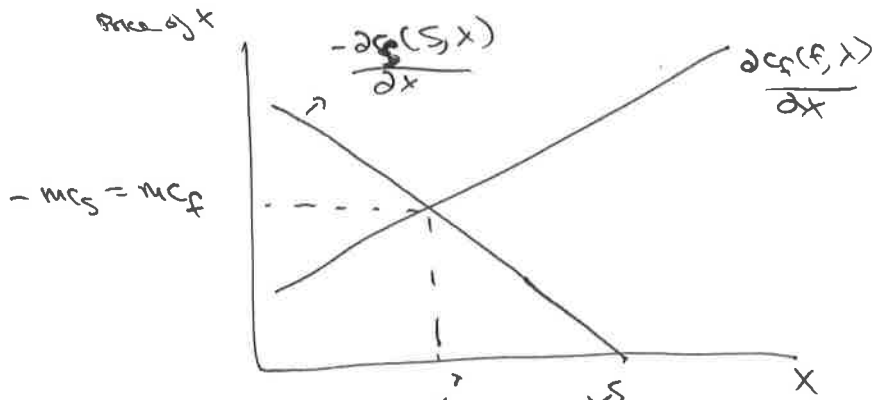
$$P_S = \frac{\partial c_S(S, x)}{\partial S}$$

$$P_f = \frac{\partial c_f(f, x)}{\partial f}$$

$$\frac{\partial c_S(S, x)}{\partial x} = \frac{\partial c_f(f, x)}{\partial x}$$

now account for how pollution affects both steel and fish production  
→ the  $x$  that solves this is the optimal  $x$

Graphically:

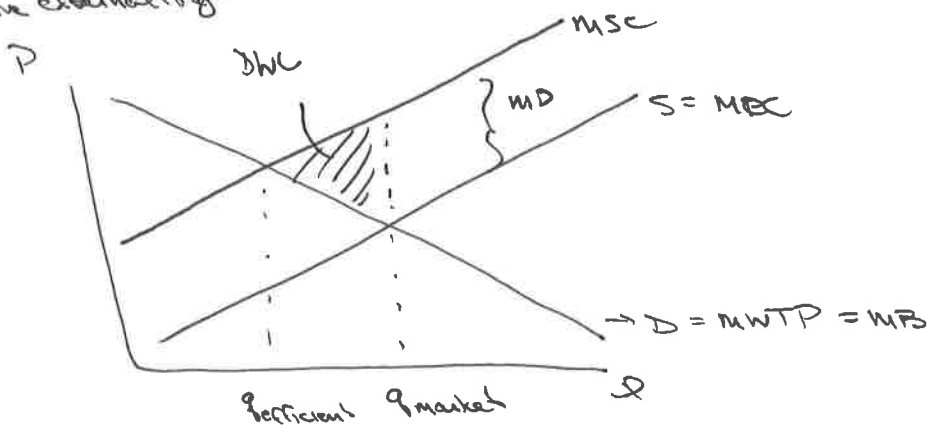


This is amount of pollution joint company

This is amount steel produced if steel company separate business

# Externalities and Market Efficiency

Negative externalities:



MP = marginal private cost

MSC = marginal social cost

MD = marginal external damage

$$MSC = MP + MD$$

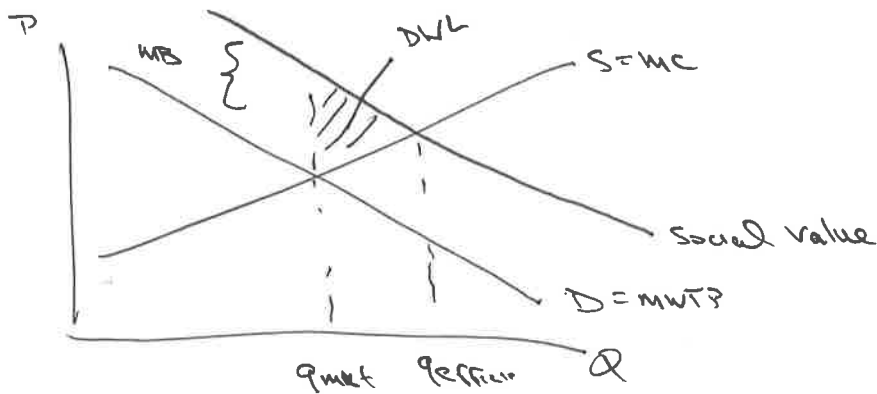
MP

→ The market only takes into account the private costs/benefits

⇒ it overproduces negative externalities

⇒ it underproduces positive externalities

e.g. positive externalities



MB = marginal external benefits

How do we solve the market failure that results in externalities?

① Define property rights more clearly (Coasian Solution)

e.g. assume fishery has right to clean water and that steel mill would need to pay fishery to pollute

→ let  $q$  be the price per unit of pollution

steel mill's problem:

$$\max_{S, X} P_S S - \underbrace{qX}_{\text{pay for pollution}} - C_S(S, X)$$

FOC's

$$① P_S = \frac{\partial C_S(S, X)}{\partial S}$$

$$② -q = \frac{\partial C_S(S, X)}{\partial X}$$

fishery's problem:

$$\max_{F, X} P_F f + \underbrace{qX}_{\text{rev from selling pollution}} - C_F(F, X)$$

FOC's

$$③ P_F = \frac{\partial C_F(F, X)}{\partial F}$$

$$④ q = \frac{\partial C_F(F, X)}{\partial X}$$

$$② \text{ \& \ } ④ \Rightarrow - \frac{\partial C_S(S, X)}{\partial X} = q = \frac{\partial C_F(F, X)}{\partial X}$$

→ optimal amount of  $X$



→ note, could define ~~the~~ right to pollute w/ steel mill  
and have fishing pay for clean water  
② → check that this yields same outcome

①

② Tax the pollution

→ we can use a tax used to correct an externality  
a Pigouvian tax

Steel mill's problem:

$$\max_{s, x} P_s s - C_s(s, x) - t x$$

↑  
tax per unit of  
x

FOCs:

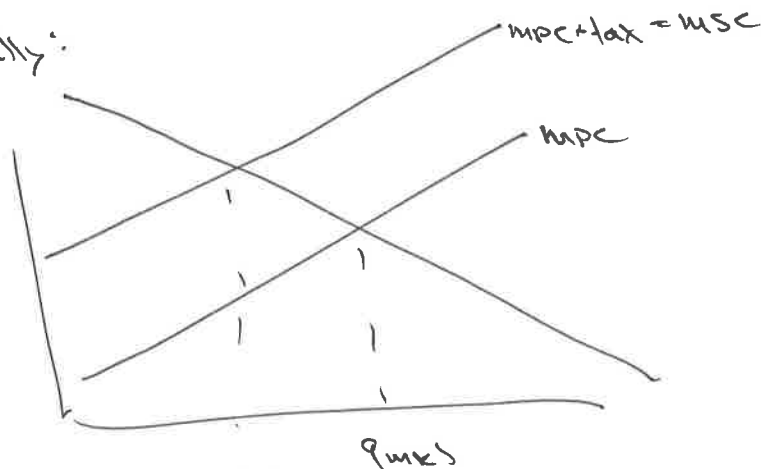
$$P_s = \frac{\partial C_s(s, x)}{\partial s}$$

$$t = -\frac{\partial C_s(s, x)}{\partial x}$$

⇒ if set  $t = \frac{\partial C_s(s, x)}{\partial x} =$  ~~the~~ marginal external damage

then get optimal pollution

Graphically:



Q<sub>MPS</sub>  
↓  
tax gets you here

③ quota

→ could reduce all firm's ~~allow~~ pollution by same amt

→ but then would cost effective

→ consider prob: want to reduce pollution across 2 firms by  $X$

→ cost of reducing pollution by  $x_1$  for firm 1 is given by  $c_1(x_1)$

→ cost of reducing pollution by  $x_2$  for firm 2 is given by  $c_2(x_2)$

$$\begin{array}{ll} \min_{x_1, x_2} & c_1(x_1) + c_2(x_2) \\ \text{s.t.} & x_1 + x_2 = X \end{array}$$

FOCs:

$$\frac{\partial c_1(x_1)}{\partial x_1} = \lambda$$

$$\frac{\partial c_2(x_2)}{\partial x_2} = \lambda$$

$$\Rightarrow \frac{\partial c_1(x_1)}{\partial x_1} = \frac{\partial c_2(x_2)}{\partial x_2}$$

equalize marginal costs of pollution abatement is most cost effective

→ so if  $c_1 \neq c_2$  then don't want  $x_1 = x_2$

→ How get the efficient outcome?

→ cap and trade

- auction off or give away permits allowing X amt of pollution
- then let firms trade permits
- outcome will look like sol'n ①

Market Signals

- An important point - the market encourages firms to internalize externalities
- They often do this → e.g. beekeeper and apple orchard,
- consider the problem of the fishery and steel mill → profits higher together than separate ⇒ gives incentive to merge to internalize costs
- Limit → this only works well for local ~~not~~ externalities

# The Tragedy of the Commons

(12)

→ The tragedy of the commons is a well known result of a production ~~externality~~ or consumption externality

→ it happens when there is a common pool resource - one that all share equally

→ in this case, no one takes into account their use of or the value to others and the resource gets over used.

→ classic example (and where name comes from) is from the problem of grazing cows on the common land.

The ~~externalities~~ problem to determine optimal # of cows:

$$\max_c f(c) - ac$$

→  $a$  = price of cow

→  $c$  = # cows

FOC:

$$\frac{\partial f(c)}{\partial c} = a \rightarrow MC = \text{price}$$

→ Each villager's problem if current output is  $f(c)$ , then per cow get  $\frac{f(c)}{c}$ .

→ Add one more cow and it gives:  $\frac{f(c+1)}{c+1}$

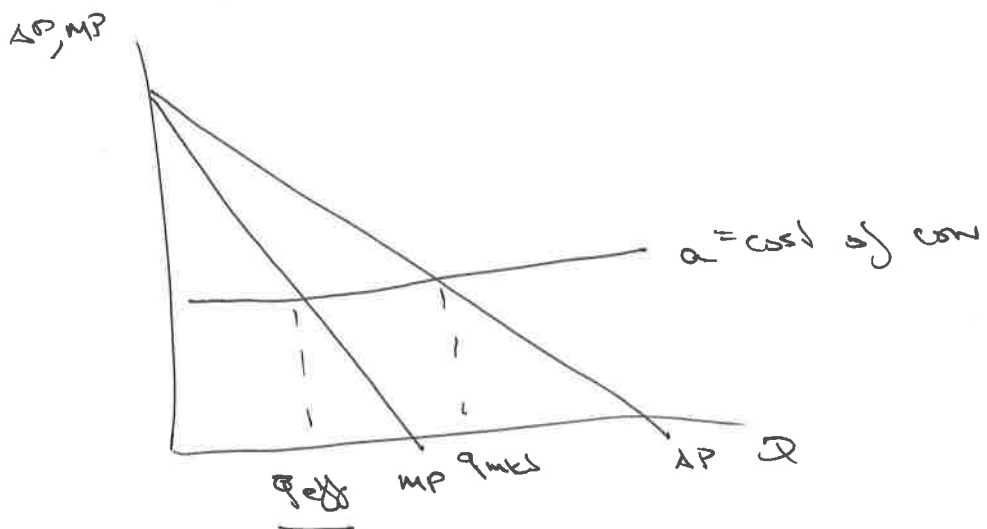
→ Add another cow if  $\frac{f(c+1)}{c+1} > a$

avg product > price

→ profits driven to zero:  $\frac{f(c)}{c} = a \Rightarrow \frac{f(c)}{c} - a = 0$   
 $\Rightarrow f(c) - ac = 0$

→ if avg prod > marg prod → too many cows

Graphically:



MP < AP b/c AP declining (so marginal must lie below the avg)

→ many examples of this:

- congestion on public roads
- fish stocks
- groundwater in dry locations (eg. Southern CA)
- Air pollution
- etc.

Pecuniary externalities

→ There are some externalities that produce external costs and benefits that offset exactly

→ we call these pecuniary externalities

→ e.g. your demand for Coke ↑ price

→ this is an external cost on other consumers

→ but that ↑ price is an external benefit to coke producers

→ the size of these ↑, the Δ in price, exactly are equal

